
Review of Special confining links in column as per IS13920-2016 and ACI318-2014

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From the past earthquake records and observations, it has been seen that many column failures during earthquake occurred due to buckling of main bars near beam column junction as there was no adequate lateral restraint. Even during the structural audit and repair works, it has been observed that confining reinforcement has not been provided in the beam column junction of RCC frames. Either in the design or during construction, some how, the confining reinforcement is missing in the junctions of beam and column and near the joints. For anticipated ductile behaviour of framed structures, confining reinforcement plays very important role and can't be ignored. The diameter of confinement reinforcement, its spacing and detailing of joints must be paid special attention for improving performance of structure during earthquake. We need to create more awareness amongst structural engineers and site engineers regarding this important provision in the code.



For ductile design and detailing of reinforced concrete structures, calculations of special confining reinforcement as per clause 7.6 of IS13920:2016 is required.

A) Factors affecting quantum of confinement reinforcement : There are various parameters that affect the amount of confinement reinforcement as cited in reference 3 like -

1. Ratio of concrete strength to tie strength f_{ck}/f_y : With the increase in concrete strength, more confinement steel is required.

2. Axial stress in concrete : Other codes consider this parameter in calculating confining steel. IS code does not account for this effect in the equation for confining reinforcement. However, IS13920 clause 7.1 puts cap on maximum axial stress in column $P_u/f_{ck} \cdot B \cdot d$ to 0.4. This may be to avoid crushing failure.

3. Unconfined cover concrete thickness : This is considered through A_g/A_k parameter where A_g is gross concrete area and A_k is area of confined concrete core.

4. Longitudinal reinforcement and its spacing – IS code does not account for this effect.

5. Curvature ductility factor – Amount of confining reinforcement in plastic hinge zone of columns has significant effect on curvature ductility as suggested by many researchers.

American code, New Zealand code, Canadian codes consider effect of axial stress in column and higher grade of concrete in calculation of confining reinforcement.

With some sample examples, comparison of confinement reinforcement in columns with IS13920:2016 and ACI318-2014 has been made.

Equating two equations given in IS code for confinement reinforcement Ash for rectangular links

$$\text{Eq (1)} \quad \text{Ash} / (\text{Sv} \cdot h) = 0.18 \cdot f_{ck} / f_y \cdot (A_g / A_k - 1) \dots\dots$$

$$\text{Eq (2)} \quad \text{or Ash} / (\text{Sv} \cdot h) = 0.05 \cdot f_{ck} / f_y \dots\dots\dots$$

whichever is higher

equating the equations, $A_g / A_k \geq 1.27$

It means second equation will govern the area of confinement links for large column sizes where ratio of $A_g / A_k < 1.27$

As the ratio of A_g / A_k is more than 1.27, it indicates effective core concrete area is less and column will not be efficient to resist the load after loss of cover concrete. Thus, the area of link is more for higher ratio of A_g / A_k .

IS code defines Ash as cross section of bar forming link where as ACI code defines volumetric ratio of area of links along each face of column considering concrete core dimension and spacing of links.

$$\text{ACI : } \text{Ash} / (s \cdot B_c) = 0.3 \cdot (f'_c / f_y) \cdot (A_g / A_k - 1) \text{ or } 0.09 \cdot (f'_c / f_y) \text{ whichever is higher.}$$

Writing the equations in IS code on similar lines of ACI code by replacing h by B_c

$$\text{IS : } \text{Ash} / (s \cdot B_c) = 0.18 \cdot f_{ck} / f_y \cdot (A_g / A_k - 1) \text{ or } 0.05 \cdot f_{ck} / f_y \text{ whichever is higher}$$

Where f'_c is cylindrical compressive strength and f_{ck} is cube compressive strength.

By substituting $f'_c = 0.8 \cdot f_{ck}$ in the expression of ACI code the factor will be $0.3 \cdot 0.8 = 0.24$.

Thus, it can be seen that confinement steel as per ACI is around 33% more than that given in IS ($0.24 / 0.18 = 1.33$) if volumetric ratio is compared from the above equations.

ACI also considers effect of axial stress ratio or higher grade of concrete in calculation of confinement steel. If the axial stress ratio $P_u / (A_g \cdot f'_c) > 0.3$ or $f'_c > 70 \text{ Mpa}$, area of hoops is further enhanced based on the number of longitudinal bars and concrete strength factor and given by expression $\text{Ash} / (s \cdot B_c) = 0.2 \cdot k_f \cdot k_n \cdot P_u / (f_y \cdot A_c h)$. This is not considered in the present IS code.

B) Effect of A_g / A_k ratio for various column sizes

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It is interesting to see the effect of A_g / A_k ratio for different column shapes. Assuming clear cover to links as 40mm, it can be seen that for square columns of size more than 700mmx700mm, the ratio of $A_g / A_k < 1.27$, thus second equation of IS code governs the area of link bar. For column size less than 700x700mm, first equation governs. The trend of A_g / A_k for square columns can be seen from Fig 1.

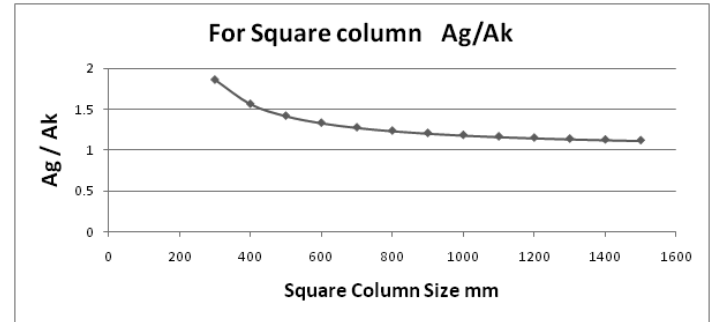


Fig 1 Variation of A_g / A_k for square columns

Considering minimum lateral dimension as 300mm as per latest code, variation of A_g / A_k can be seen for walls of 300mm thickness and 400mm thickness from Fig2. It can be seen from the figure that the ratio does not go below 1.27 though it reduces as the wall length is increased. Since the ratio of A_g / A_k does not fall below 1.27, equation 1 as given in IS13920 will always govern for confining reinforcement for all the walls.

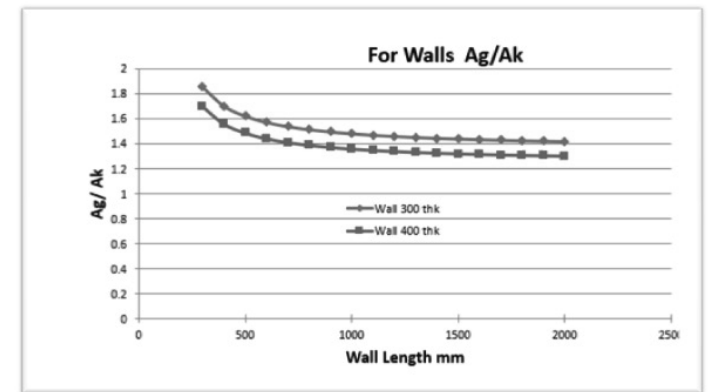


Fig 2 Variation of A_g / A_k for walls of 300mm thickness and 400mm thickness.

c) Sample calculations for confining reinforcement as per IS and ACI code for different columns

Case 1) Column of dimension 400mm x 1100mm

Consider following column details as shown in Fig3.

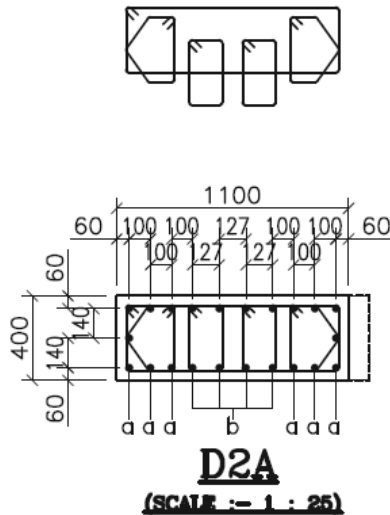


Fig 3 Rectangular column 400mm x1100mm

From consideration of ease of concreting, spacing of links should not be less than 100mm. Thus, considering spacing of links as 100mm. As per the equation given in code IS13920:2016 Clause 7.6

Ash area of bar forming link is given by higher of

$$Ash = 0.18 * Sv * h * fck / fy * (Ag / Ak - 1)$$

$$Or = 0.05 * Sv * h * fck / fy$$

Considering M35 concrete, $F_y = 500$ Mpa

$S_v = 100$ mm minimum (considering ease of placing of concrete)

$$A_g = 400 * 1100 = 440000 \text{ mm}^2$$

$$A_k = (400 - 2 * 40) * (1100 - 2 * 40) = 326400 \text{ mm}^2$$

$$A_g / A_k = 440000 / 326400 = 1.348$$

IS Code mentions h as longer dimension of rectangular link but does not exceed 300mm which is a bit confusing. It should have been distance between the longitudinal bars which are tied by cross link as per ACI which sounds more rational.

In the above case, distance between longitudinal bars varies from 100mm to 140mm. Code should clarify on value of h to be considered in the calculations. If the main bar distances are variable for a given column bar arrangement, whether one should consider average of all the bar distances for calculations of h which is more logical.

$$h(\text{average}) = (2 * 140 + 3 * 127 + 6 * 100) / 10 = 126 \text{ mm}$$

Value of Ash is influenced by value of h .

$$Ash = 0.18 * 100 * h * 35 / 500 * (1.34 - 1) = 0.43h$$

For different values of h , value of Ash is as below –

For 100mm Ash = 43.8mm² (8mm link is Ok)

For 126mm Ash = 54mm² (10mm link is required)

For 140mm, Ash = 61.3mm² (10mm diameter of link is required)

For 200mm Ash=87.6mm² (12mm link is required)

For 300mm, Ash =131 mm² (16mm diameter link is required.)

In short, we will not be able to use 8mm links any more in most of the cases.

Calculations checked with ACI318-2014 provisions –

As per Table 18.7.5.4

For rectangular hoop $R_{st} = n * A_b / s * B_c = 0.3 (f'c / f_y) (A_g / A_c - 1)$ or $0.09 (f'c / f_y)$ which ever is higher.

Where n = number of legs of hoop

A_b = area of one link bar

S = spacing of links

B_c = width of column perpendicular to link

$f'c$ = cylindrical strength = $0.8 * f_{ck}$

Calculations to be performed along the width and length of column face and higher value is to be considered.

Considering calculations along the width = $400 - 2 * 40$ cover = 320mm = B_c

Number of effective legs of link in width $n_1 = 2$ straight + $0.7 * 2$ inclined = 3.4 nos

Considering link spacing of 100mm = S

Using above equation

$$3.4 * A_b / (100 * 320) = 0.3 * (0.8 * 35 / 500) (1.34 - 1)$$

Thus $A_b = 53 \text{ mm}^2$, Thus 8mm link is just OK at 100mm spacing.

Considering calculations along the length $B_c = 1100 + 2 * 40 = 1020$

$n_2 = 8$ straight + 2 inclined * $0.7 = 9.4$

Using the same equation

$$9.4 * A_b / (100 * 1020) = 0.3 * (0.8 * 35 / 500) (1.34 - 1)$$

Thus $A_b = 62 \text{ mm}^2$.

Higher value of 62 mm² is to be considered. Thus, 10mm link is required at 100mm spacings.

Comparing volumetric ratio of links as per both codes -

Volumetric ratio as per ACI Ash/ S. Bc = 0.3 (f'c/ fyt) (Ag/Ac -1) =

$$= 0.3 * (0.8 * 35 / 500) (1.348 - 1) = 0.005846$$

Volumetric ratio as per IS code Ash/S. Bc = 0.18 * fck/fy *(Ag/Ak -1)

$$= 0.18 * 35 / 500 * (1.348 - 1) = 0.00438$$

As per ACI318 , If the axial stress ratio Pu/Ag*f'c > 0.3 volumetric ratio is governed by

Ash / (s. Bc) = 0.2 * kf * kn * Pu / (fyt * Ach) which means , confining reinforcement is increasing with increasing axial stress ratio.

Plotting the values for the same column as given in Figure 4

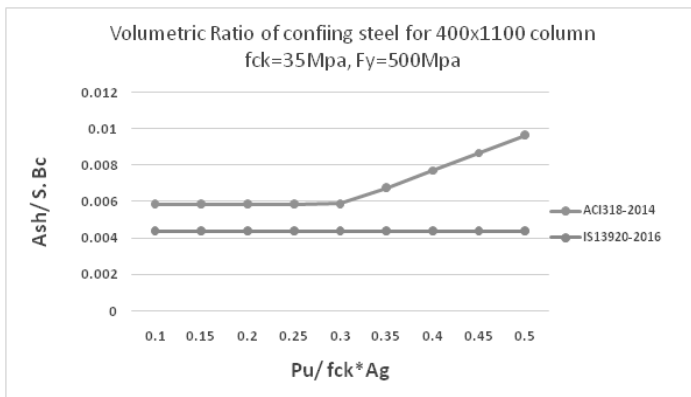


Fig 4 Volumetric ratio of confining steel v/s axial stress ratio in column

Case 2) For 600mm x 600mm column

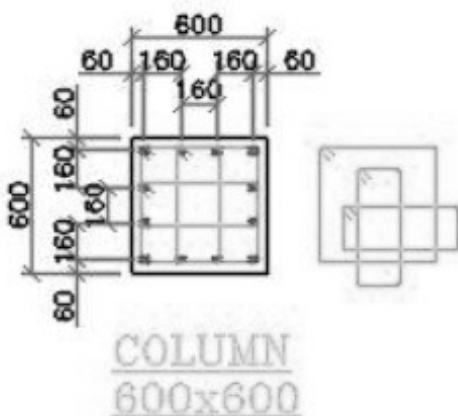


Fig 5 square column of 600mm x600mm size

Main longitudinal bars 12 nos as shown in the arrangement. The link required can be calculated as

$$A_g = 600 \times 600 = 360000 \text{ mm}^2$$

$$A_k = (600 - 80) \times (600 - 80) = 270400 \text{ mm}^2$$

$$A_g / A_k = 360000 / 270400 = 1.33$$

M35, Fe500, Sv=100mm, longer side of link h=160mm+20mm main bar +8 link*2 = 196mm

Area of link Ash = 0.18 * 100 * 196 * 35 / 500 (1.33-1) = 81.4mm² (we need more than 10mm diameter as link)

If area of link is calculated considering volumetric ratio as per ACI Concept

h= average spacing of long bar in the width = (600-2*40) / 4 legs of link =130mm av

Area of link Ash= = 0.18 * 100 * 130 * 35 / 500 (1.33-1) = 55 mm²

Considering calculations as per ACI318-2014 for 100mm spacing of links -

$$n=4$$

$$B_c = 600 - 2 * 40 = 520 \text{ mm}$$

$$A_g / A_c = 1.33$$

Using the equation for area of link -

$$n * A_b / s. B_c = 0.3 (f'c / f_{st}) (A_g / A_c - 1)$$

$$4 * A_b / (100 * 520) = 0.3 * (0.8 * 35 / 500) (1.33 - 1)$$

Thus , area of link required A_b= 72mm²

Case 2 A For 300x300mm column

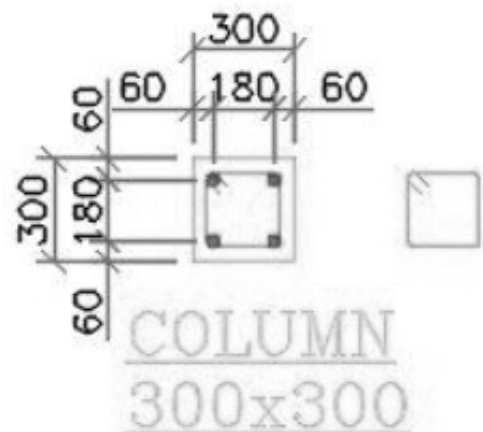


Fig 6 Square column 300mm x300mm

with 4 main bars of 25mm diameter, the link required can be calculated as

$$A_g = 300 \times 300 = 90000 \text{ mm}^2$$

$$A_k = (300 - 80) \times (300 - 80) = 48400 \text{ mm}^2$$

$$A_g/A_k = 90000/48400 = 1.85$$

M35, Fe500, Sv=100mm, h=300-2*40cover = 220mm

$A_{sh} = 0.18 * 100 * 220 * 35 / 500 (1.85 - 1) = 235 \text{ mm}^2$ (we need more than 16mm diameter as link ... which is not feasible to provide at site)

If the same calculations are done on volumetric ratio based on ACI concept, i.e. two legs of link in the width of 220mm, effective width of each link = $220/2 = 110 \text{ mm}$ and $A_{sh} = 235/2 = 120 \text{ mm}^2$ which sounds more rational.

Considering calculations as per ACI318-2014 for 100mm spacing of links -

$$n = 2$$

$$B_c = 300 - 2 * 40 = 220 \text{ mm}$$

$$A_g/A_c = 1.85$$

Using the equation for area of link -

$$n * A_b / s * B_c = 0.3 * (f'c / f_y) * (A_g/A_c - 1)$$

$$2 * A_b / (100 * 220) = 0.3 * (0.8 * 35 / 500) * (1.85 - 1)$$

Thus $A_b = 157 \text{ mm}^2$

Case 3) For 600mm diameter circular column

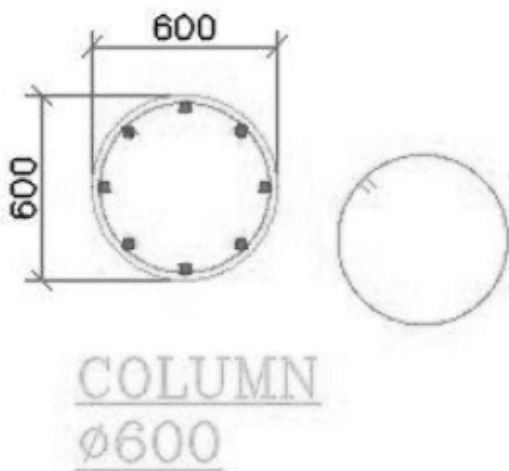


Fig 7 Circular column 600mm diameter

$F_{ck} = 35 \text{ Mpa}$; $F_y = 500 \text{ MPa}$; Cover 40mm to link and pitch of spiral assumed as 100mm

$$A_g = 3.142/4 * 600^2 = 282780 \text{ mm}^2$$

$$D_k = 600 - 2 * 40 = 520 \text{ mm}$$

$$A_c = 3.142/4 * (600 - 2 * 40)^2 = 212399 \text{ mm}^2$$

$$A_g/A_c = 282780/212399 = 1.33$$

As per IS13920-2016

$$A_{sh} = 0.09 * s * D_k * f_{ck} / f_y * (A_g/A_c - 1) = 0.09 * 100 * 520 * 35 / 500 * (1.33 - 1) = 108 \text{ mm}^2$$

As per ACI 318-2014

$$R_{st} = n * A_b / (S * D_k) = 0.45 * (f'c / f_y) * (A_g/A_c - 1)$$

$$n = 4$$

$S = 100 \text{ mm}$ spacing, $D_k = 520 \text{ mm}$, $f'c = 0.8 F_{ck}$

$$4 * A_b / (100 * 520) = 0.45 * (0.8 * 35 / 500) * (1.33 - 1)$$

Thus, area of hoop $A_b = 108 \text{ mm}^2$, same as that of IS code calculations.

D) Trends for confining reinforcement as per IS code equations

A graph for value of A_{sh} for circular column can be plotted for various parameters like $F_{ck} = 35 \text{ MPA}$, $F_y = 500 \text{ Mpa}$ and considering pitch of spiral as 75mm. It can be seen from the graph that the direction of graph changes at 700mm diameter where $A_g/A_k = 1.27$. Beyond 700mm diameter, A_{sh} increases with the diameter of column. More than 10mm diameter hoop will be required.

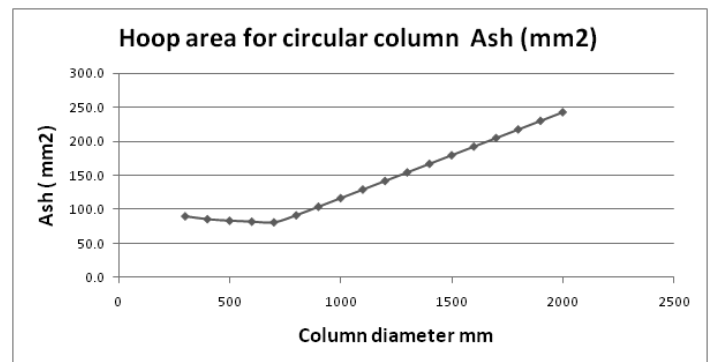


Fig 8 Hoop area for circular column with 75mm pitch, $F_{ck} = 35 \text{ MPa}$, $F_y = 500 \text{ Mpa}$

Similarly, trend for confining reinforcement for square column can be plotted considering $F_{ck} = 35 \text{ MPA}$, $F_y = 500 \text{ Mpa}$. Area of link A_{sh} will be a function of h (which is the distance between the

longitudinal bars but less than 300mm). In IS code it is defined as longer dimension of rectangular link but does not exceed 300mm.

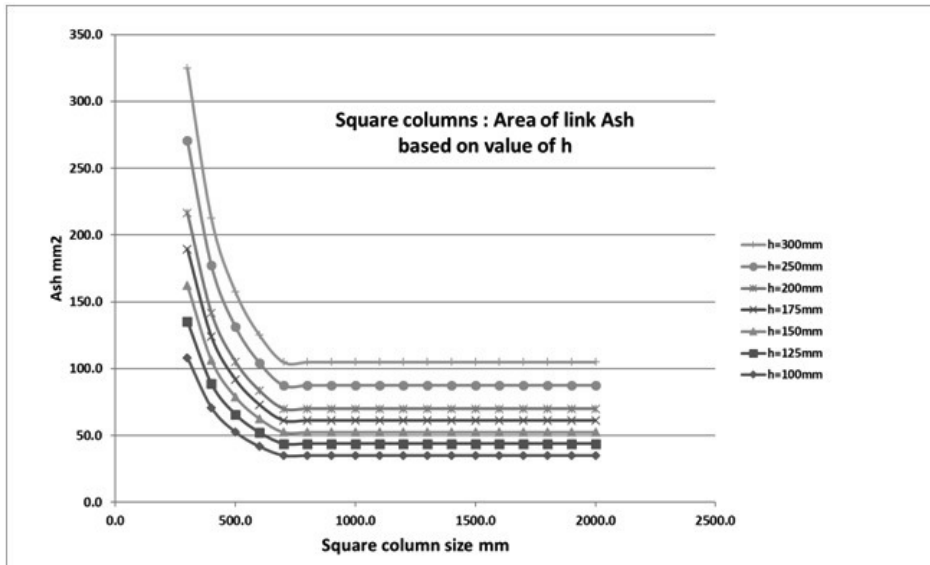


Fig 9 Area of link Ash for square columns with variable h for $F_{ck}=35\text{Mpa}$, $F_y=500\text{Mpa}$, link spacing 100mm

Thus, from the graphs in Fig 9, it can be observed that for the main bar spacing up to 200mm, hoop of 10mm diameter will be required for column size above 600mm and 8mm hoop may be enough if the main bar spacing is less than 150mm.

Trend for confining reinforcement for columns / walls of 300mm thickness has been shown in Fig10 for various values of h (which is the distance between the longitudinal bars but less than 300mm) and for $F_{ck}=35\text{Mpa}$, $F_y=500\text{Mpa}$

It can be seen from Fig10 that 8mm diameter link

is not enough for walls. Minimum 10mm diameter link will be required if the spacing of main bars is restricted to 125mm. Higher diameter links will be required if spacing of main reinforcement is increased. Thus, to restrict the link diameter , it is necessary to keep spacing of main bars within 150mm.

For the same cross section area of column (concrete area 0.36m^2) and same main steel (around 1.65%) , theoretical consumption of confining reinforcement is compared as per IS code

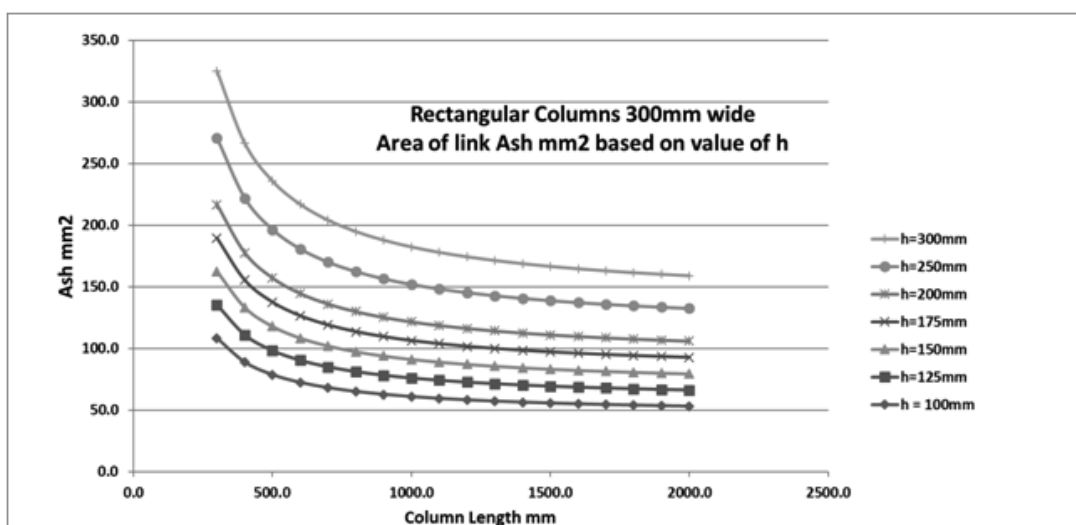


Fig 10 Area of link Ash for 300wide column / walls with varying h for $F_{ck}=35\text{Mpa}$, $F_y=500\text{Mpa}$, spacing of links $S_v=100\text{m}$

considering various shapes of columns considering parameters like spacing of links as 100mm, cover 40mm, $F_{ck} = 35\text{Mpa}$, $F_y=500\text{MPa}$ and h as centre to centre distance between main bars. The calculations are presented in Table1 . Similar comparison can be done for various column shapes and bar arrangements.

Table 1 : Consumption of confining reinforcement in columns.

Sr.no	Column size	Main steel	Area of link Ash mm ²	Length of links in m	Weight of links steel Kg / m ³ of conc.
1	Circular 677mm diameter	12 nos Tor 25	108 mm ²	1.82 m	44 kg/m³
2	Square column 600mmx600mm	12 nos Tor 25	67 mm ²	5.33 m	77 kg/m³
3	Rectangular 300mm x1200mm Main bars on long side	20 nos Tor 20	70 mm ²	5.67 m	96 kg/m³
4	Rectangular 300mm x1200mm Main bars on long side	12 nos Tor 25	156 mm ²	4.77 m	177 kg/m³

Order of preference for column shape for having minimum weight of links will be circular, square, rectangular and walls with minimum spacing of main bars. Circular columns will require minimum weight of links and walls will have maximum.

Conclusions :

1. For rectangular and square columns, it is necessary to simplify the IS code equation of confining reinforcement on volumetric basis as given in ACI which leads to more rational calculations.
2. More clarity is required in the definition of h in IS 13920 for calculation of confining reinforcement. In practice, spacing between the main column bars is not constant. To avoid any confusion on longer side of link, h can be considered to be the average distance between the longitudinal column bars which are laterally tied.
3. For circular column, hoop diameter increases with diameter of column. Links of 10mm and higher diameters will be required.
4. In most of the building projects, 8mm diameter links are still being used for columns and walls which is not sufficient as per the code guidelines. We need to switch to 10mm diameter and higher bars for links as per the requirements. Link diameter is governed by spacing of main column bars.
5. For the same cross section of concrete and main steel, weight of links will be minimum

for circular sections and will be maximum for walls.

6. It is necessary to create more awareness among structural engineers and site engineers to provide correct confinement reinforcement which will improve performance of our RCC structures.

References :

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